Discussion on Comparing Machine Learning Models for Health Outcome Prediction

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Abstract: This position paper argues the need for more details than simple statistical accuracy measures when comparing

> machine learning models constructed for patient outcome prediction. First, statistical accuracy measures are briefly discussed, including AROC, APRC, predictive accuracy, precision, recall, and their variants. Then, model correlation plots are introduced that compare outputs from two models. Finally, a more detailed analysis of inputs to the models is presented. The discussions are illustrated with two classification problems

in predicting patient mortality and high utilization of medical services.

INTRODUCTION

There is a significant recent growth in the use of Machine Learning (ML) methods in medical, healthcare and health applications. These applications span from patient risk stratification (Tseng et al., 2020; Beaulieu-Jones et al., 2021), to differential diagnosis (Castellazzi et al., 2020; Vaccaro et al., 2021), to image recognition and analysis (Rahane et al., 2018; Saha et al. 2021). The application of ML methods achieved incredible results that often outperform human experts. This growing interest is followed by strong opposition to the use of ML and criticism of the methods. Among the most often cited criticisms are lack of reproducibility of results (McDermott et al., 2021), biases in constructed models, sometimes referred to as lack of fairness (Mehrabi, 2021), and lack of transparency.

The context of the presented work is supervised learning from medical or health data applied to prediction of patient outcomes. Such data can consist of medical claims, electronic medical records, registries, surveys, and all other types of data, but can be applied beyond healthcare. In our 2021 HEALTHINF presentation (Wojtusiak, 2021), we argued the need for detailed reporting of results when presenting outcomes of ML modeling of healthrelated problems. That work identified ten MLI

criteria for reporting results: (1) experimental design, (2) statistical model evaluation, (3) model calibration, (4) top predictors, (5) global sensitivity analysis, (6) decision curve analysis, (7) global model explanation, (8) local prediction explanation, (9) programming interface and (10) source code. Although not always sufficient, these criteria are argued to be necessary to describe constructed models and allow for reproducibility of results.

Different questions arise when one needs to compare two or more models. Is it sufficient to compare models based on their performance (accuracy) only? Should one use all of the above ten criteria to compare models? Are some additional tests needed to understand differences between models? And most importantly: what does it actually mean that one model is better than another?

There is surprisingly little literature that present frameworks for comparing ML models. When searching for published works on comparison of ML models, all papers that appear are comparing specific models (or algorithms) for solving specific problems at hand. Virtually all of them report only some statistical measures discussed here in Section 3. Similarly, large number of "data science" websites discuss practical aspects of comparing models, including examples of source code, but also limit these comparisons to statistical accuracy measures.

There are approaches available in other fields. Lee and Sangiovanni-Vincentelli (1998) presented a general framework for comparing computation methods. While their work is applicable to the problems presented here, they do not provide practical insights.

The concepts presented in this paper are described in context of classification learning problems, and most often binary classification, but can be generalized to multiclass problems as well as regression.

The discussed approaches are illustrated in terms of two supervised learning problems, which are constructed to predict patient outcomes using medical claims data. More specifically, medical claims for five percent control set of the linked Medicare beneficiaries from the Surveillance, Epidemiology, and End Results (SEER)-Medicare dataset between 1995 and 2013 were used to construct the models. The Medicare claims collected by Medicare and Medicaid Services (CMS) provide one of the largest longitudinal datasets for the Medicare eligible population (aging population) in the United States. Two classification problems were established for predicting one-year mortality (Problem 1), and high utilization of medical services (Problem 2). For both problems, the inputs were derived from data before year 2013 and the outcomes were calculated in 2013. Participants in the cohort were at least 70 years old and alive on January 1st, 2013. Patients' demographic information including age and race as well as their diagnosis codes collected over the course of 18 years were used to create models. In this study, diagnosis codes in the form of nineth revision of the International Classification of Diseases (ICD-9) codes were transformed into 282 clinically relevant categories using Clinical Classification Software (CCS) codes. A binary outcome was created for Problem 1 indicating whether or not the patient died by the end of 2013. In Problem 2, patients who had total number of claims exceeding the 90th percentile in 2013 were considered high utilizers in defining the binary outcome of high utilization.

The final dataset included 83,590 patients in which 10% of the population were high healthcare utilizers and about 7% of the cohort died in 2013. The majority of patients in the cohort were white, and the average age was 79. All patients were male.

In the presented work, the requirement (1) for model comparison is the ability to apply models to the same cases in order to compare results. In practice, this means that the test sets used to evaluate models are derived from the same database, or different databases linked by a common identifier. For example, one model can be built from EHR data and another from claims data. The models can still be

compared if the EHR and claims data are linked to the same cases using common identifier. Further, this means that (2) the models need to be based on the same unit of analysis, i.e., each row in the test datasets corresponding to the same objects. Finally, (3) outputs from the models need to be the same. For example, when one model predicts the probability of high utilization of medical services, the other model must predict the same output (and not for example time to the next hospitalization). While one can argue about the possibility of relaxing the requirement (3) to a certain degree for simplicity this paper assumes that all three conditions are held.

The content of Sections 2 and 3 of this paper is mainly informative and reflect comparisons presented in most published works. The methods described in Section 4 has been used by the authors for several years but are not present in mainstream literature. Finally, the comparisons described in Section 5 have not been previously discussed.

2 MODEL CONSTRUCTION

The presented work focuses on models constructed by supervised machine learning. Construction of such models follows two main steps: data preprocessing and application of ML algorithms as shown in Figure 1. Even small changes at any step of model construction can have a drastic impact on the results. The process of finding the best set of settings in model construction is called model tuning or hyperparameter tuning. Interestingly, most researchers only consider hyperparameter tuning as optimization of learning algorithm, while keeping fixed preprocessing steps (or optimizing them separately/manually). Changes to the representation space resulting from data preprocessing result in very different types of changes to the models than those resulting from tuning hyperparameters.

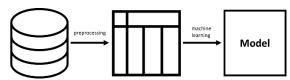


Fig 1: From raw data to preprocessed data to model.

Let's consider models M_1 , M_2 , ... M_k that classify or predict the same targets (i.e., the models are intended to solve the same problem). For simplicity, let's assume that these models are intended for binary classification.

$$M_i(X^i) \rightarrow \{0,1\}$$

For each representation space X^i , there needs to be a transformation $\Phi^i(DB) \to X^i$ from the original data to that specific representation. That transformation involves all the steps required to convert raw data into one that can be directly used by ML algorithms and models.

There are several cases to consider. When $X^i = X^j$, the same preprocessing can be applied to both representations, and the differences in models M_i and M_j is in the learning algorithms or their hyperparameters. Similarly, when $X^i \neq X^j$, different preprocessing steps were applied to obtain the two representations. For example, raw claims data can be transformed into binary representation in which presence/absence of diagnoses is represented as $\{0,1\}$ or into Temporal Min-Max representation in which time from the first known and the most recent occurrence of a diagnosis are represented (Wojtusiak et al., 2021a,b).

3 STATISTICAL MEASURES

The standard in model comparison is based on statistical accuracy measures of the models. For classification problems, Area Under Receiver-Operator Curve, denoted as AROC or sometimes simply AUC (Hanley & McNeil, 1982; Fawcett, 2006) is the most frequently used measure in biomedical and health informatics literature, followed by predictive accuracy, recall (sensitivity) and precision (Powers, 2020). In biomedical literature sensitivity and specificity are typically used instead of recall and precision. Many authors combine precision and recall into a single F1-score (Goutte & Gaussier, 2005). In the published literature, these measures are used to report results of modeling efforts, but also when performing hyperparameter tuning to achieve the highest accuracy, AUC or F1score. Other metrics are also used such as Area Under Precision-Recall Curve (AUCPR) (Boyd et al., 2013), Kappa Statistic (McHugh, 2012), relative entropy, mutual information and others (Baldi et al., 2000).

Most notably these measures are not typically used by the learning algorithms whose "internal" measure of fit is defined by a loss function. Loss functions combine some metrics of accuracy with additional terms used for regularization. Large number of loss functions have been investigated in ML and recently most often in the context of neural networks (Wang et al., 2020).

To exemplify these most popular measures, let's consider four algorithms applied to prediction of 1-

year mortality (Problem 1): Random Forest (Breiman, 2001), Gradient Boost (Friedman, 2001; Friedman, 2002), and Logistic Regression (Hosmer et al., 2013), and Decision Tree (CART algorithm) (Breiman et al., 2017; Batra & Agrawal, 2018). ROC Curves for the four methods are shown in Fig. 2. Several things are clear from the figure. The curves for GB, RF and LR models are visually close to each other with GB slightly dominating the other two. This is also evident when calculating AROC for the three models AROC(GB)=0.8, AROC(RF)=0.78, and AROC(LR) = 0.76. The differences are statistically significant with p<0.05 for t-test over 10-fold crossvalidation. It is also clear that at certain levels of threshold, GB and RF algorithms perform identically when the lines overlap.

It is also clear that ROC is ill-defined and AROC should not be calculated for decision tree-based models that do not provide probabilistic output but only the final decision. Literature often presents ROC curves for decision trees or decision rules with collected lines as in Fig 2, but this is also misleading, as only one point exists on the curve. One can argue that pruned DTs return scores in [0,1] range, but it is our belief that AROC should not be used for them either.

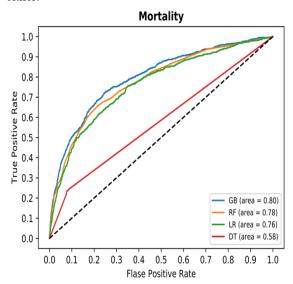


Fig 2: Receiver Operator Curves for four algorithms in predicting 1-year patient mortality.

Similarly, one can compare different models constructed with different representation spaces as illustrated in Fig. 3. It shows ROCs for GB-based models with Binary and Temporal Min-Max representation. Here, it is clear that the temporal representation is superior at every possible classification threshold.

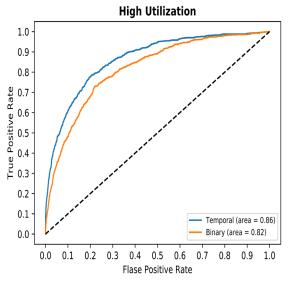


Fig. 3. Receiver Operator Curves comparing two representation spaces in predicting high utilization of medical services.

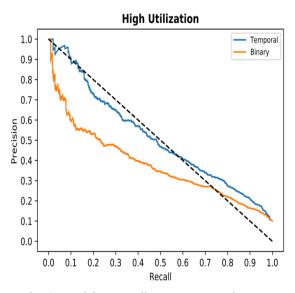


Fig. 4. Precision-Recall Curves comparing two representation spaces in predicting high utilization of medical services.

Some authors argue the benefit of using Precision-Recall Curves (PRC) and AUCPR instead of AROC. An example of such curves is shown in Fig. 4 in predicting high utilization (*Problem 2*) using GB.

Precision and recall (and F1-score) are calculated for one specific point on the PRC, which corresponds to a threshold that is selected by the application. Interestingly, few works report precision and recall for classification thresholds other than 0.5, which makes the direct comparison of models often impossible based on the two measures. One model may have higher precision, while other has higher recall. While F1-score solves the problem by calculating a single number, it is an oversimplification. Thus, it is suggested to fix value of one of the measures and report the other. For example, precision can be reported at recall of 90% of both models, or conversely recall can be reported at precision of 90%.

Calibration (Fig. 5) refers to the property of models that compare their output probability to the actual probabilities as defined by frequencies of positive and negative examples. Numerically, calibration is quantified with Briar score, that is mean squared error between scores and probabilities (Flach, 2019).

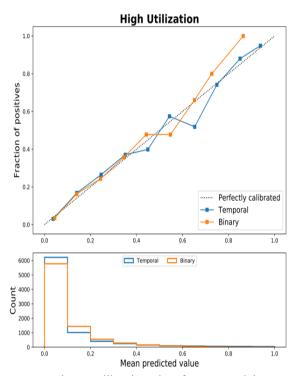


Fig 5. Calibration plots for two models constructed using Temporal Min-Max representation and binary representation.

Finally, it is important to compare models' performance for specific sub-populations. ROC and PRCs as well as calibration can be investigated. The model performance analysis on sup-population has been popularized with the growing focus on fairness in Artificial Intelligence (AI). In short, one needs to check if model accuracy is comparable for sub-populations, especially those representing minorities and vulnerable populations.

4 OUTPUT COMPARISON

Comparing calibration of models gives good insight about their outputs and allows for some comparison at different output levels. However, neither calibration analysis nor any of the other statistical methods described in Section 2 provide case-by-case insights into models' performance.

Model Correlation Plots (MCP) allow for visual case-by-case comparison of model outputs (Wojtusiak et al., 2017). The MCPs are scatterplots with axis corresponding to outputs of two models, and points representing individual cases (i.e., patients) for which predictions are made. If two models are identical, all points are located at the diagonal and MI(x) = M2(x) for every x in dataset (training or testing). Further, MCPs encode true class by color or symbol as shown in Fig. 6, which in this case red points represent high utilizers and green non-high utilizers, and may include regression lines.

The corresponding aggregated data are presented in Table 1 for both mortality and high utilization prediction problems. Wilcoxon signed-rank test was used to compare the results and significance in differences is indicated in Table 1.

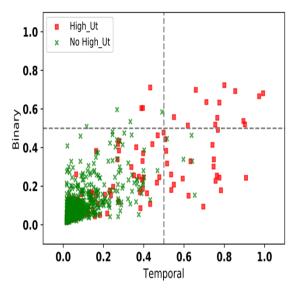


Fig 6. Model Correlation Plot that compares two Gradient Boost models based on Binary and Temporal Min-Max representations in predicting high utilization of medical services.

When observing values in Fig 6, it is clear that both sets are nonempty with large number of cases. It can be also observed that the Temporal Min-Max-based model tends to produce overall higher scores for positive test cases. The average output probability among cases with positive labels was significantly

higher across Temporal Min-Max representationbased models (also shown in Table 1). Overall, higher probabilities of positive labels and lower probability of negative labels in Temporal representation suggest that this method is generally more likely to correctly classify both classes. Also, higher recall in Temporal representation of diagnoses suggests that the method allows the algorithms to select more positive cases that are missed in Binary representation method, thus leading to overall higher recall (Table 2).

Table 1: Comparison of output probability for Temporal Min-Max (Tem) vs. Binary (Bin) Representations. * indicates significance (p<0.05).

Problem 1 - Mortality					
	Positive Label			Negative Label	
Alg	Temp	Bin	Temp	Bin	
RF	.1859*	.1459	.0758*	.0765	
GB	.1883*	.1452	.0637*	.0674	
LR	.1579*	.1487	.0665*	.0673	
Problem 2 – High Utilization					
RF	.3040*	.2300	.0879*	.0946	
GB	.3282*	.2385	.0748*	.0850	
LR	.2680*	.2414	.0817*	.0848	

Table 2: Comparison of the number correct classified cases for Temporal Min-Max vs.

Problem 1 - Mortality					
Positive Label Negative Label					
Alg	Temp	Bin	Temp	Bin	
RF	143	8	16	75	
GB	465	33	67	348	
LR	99	28	78	159	
DT	980	715	5244	4767	
Problem 2 – High Utilization					
RF	1115	118	174	417	
GB	1443	196	418	811	
LR	524	167	240	439	
DT	1902	1114	6133	5031	

Let's consider two models M_1 and M_2 . Let TS_1 be a set of examples from the test set TS such that $\bigvee_{x \in TS_1} M_1(x) > M_2(x) + \varepsilon$. Similarly, one can define TS_2 as $\bigvee_{x \in TS_1} M_1(x) < M_2(x) - \varepsilon$. The sets TS_1 and TS_2 define points for which the models

produce higher scores retrospectively. Instead of counting correct/incorrect cases or calculating precision and recall, one can compare examples in sets TS_1 and TS_2 . This analysis can be further stratified by patient demographics and plots constructed separately for genders, races, age groups, or different diagnoses. On aggregate, this is equivalent to calculating Mean Squared Error or Mean Absolute Error from the 0/1 classification methods.

5 INPUT COMPARISON

Comparing model outputs allows for visually or statistically inspecting differences between models on individual cases. However, one needs to understand if there are any patterns within input values that correspond to differences in outputs of the compared models. In other words, are there patterns in input values that correspond to outputs visualized in model correlation plots? The patterns can be described in terms of attributes present in the data or derived from them.

Let TS^+ be a set of positive cases in testing set TS and TS^- be a set of negative cases in TS. Let's consider now four subsets of the testing set.

$$\begin{array}{l} CPM_1 = \{x \in TS^+ \colon M_1(x) \geq \tau \land M_2(x) < \tau\} \\ CNM_1 = \{x \in TS^- \colon M_1(x) < \tau \land M_2(x) \geq \tau\} \\ SPM_1 = \{x \in TS^+ \colon M_1(x) \geq M_2(x) + \varepsilon\} \\ SNM_1 = \{x \in TS^- \colon M_1(x) < M_2(x) - \varepsilon\} \end{array}$$

 CPM_1 and CNM_1 are respectively positive and negative cases correctly classified by model M_1 but not M_2 . SPM_1 and SNM_1 are positive and negative cases better classified by model M_1 . These four sets can be compared in terms of values of input attributes. The sets CPM_2 , CNM_2 , SPM_2 , and SPM_2 are defined analogously for results superior by model M_2 .

For example, let's consider again the two problems of predicting mortality and high utilization for medical services. Let M_1 be model based on Temporal Min-Max representation and M_2 model based on standard Binary representation. One simple way to assess patient risk for both problems is a simple count of underlying medical conditions (present diagnosis codes). For all cases correctly classified by one model but incorrectly by another, what are the counts of present medical conditions. These numbers are reported in Table 3. Note the extremely small value 1.1 for Binary representation in random forest classifier. That number is due to very small number of cases correctly classified when using Binary representation and incorrectly with Temporal Min-Max representation. Similarly, Table 4 presents values for cases better predicted by one of the models.

Table 3: Comparison of the number of present codes for Temporal Min-Max vs. Binary representations for correct predictions.

Problem 1 - Mortality					
		e Label S ⁺	Negative Label TS ⁻		
Alg	Temp CPM ₁	Bin CPM ₂	Temp CNM ₁	Bin CNM ₂	
RF	83.0*	1.1	10.5*	77.3	
GB	77.9	87.0	85.8*	78.5	
LR	80.0	86.5	84.9*	78.8	
DT	68.9*	65.0	57.8*	59.5	
Problem 2 – High Utilization					
RF	85.3*	103.7	101.5*	88.9	
GB	79.7*	97.0	96.8*	80.8	
LR	85.8*	99.7	98.1*	85.6	
DT	76.9*	78.6	63.6*	64.0	

Table 4: Comparison of the number of present codes for Temporal Min-Max vs. Binary representations for superior predictions.

$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	Problem 1 - Mortality					
Alg SPM1 SPM2 SNM1 SI RF 60.68° 52.52 46.25° 50 GB 60.52° 52.92 47.71° 40 LR 57.35 57.08 49.19° 40 DT 68.46° 64.24 56.89° 50	Negative Label TS ⁻					
GB 60.52* 52.92 47.71* 44 LR 57.35 57.08 49.19* 4. DT 68.46* 64.24 56.89* 55	Bin √M ₂					
LR 57.35 57.08 49.19 4. DT 68.46* 64.24 56.89* 55).13					
DT 68.46* 64.24 56.89* 58	5.23					
	5.13					
Problem 2 – High Utilization	3.49					
	Problem 2 – High Utilization					
RF 71.74* 70.50 47.24* 50	0.83					
GB 70.70 70.99 49.22* 39	9.08					
LR 69.72° 72.65 44.79° 4.	5.71					
DT 76.84* 78.54 62.85 65	3.19					

Diving deeper into comparison of the models constructed with Binary and Temporal Min-Max representations, it is possible to compare the actual values within cases based on these representations. Temporal Min-Max representation has more information than binary representation, and more specifically the numbers of days. Thus, a reasonable comparison is one that looks at numbers of days from diagnoses for cases correctly classified by either of the models (but not both) as shown in Table 5, or better predicted by either of the models as shown in

Table 6. The structure of these tables is analogous to the Tables 3 and 4, but values are average numbers of days between diagnosis and prediction.

Depending on the actual types of models constructed and the representation spaces used, one needs to design appropriate comparisons on input values. These depend on the nature of data, such as static or temporal, types of input attributes, numbers of attributes, and types of models used.

Table 5: Comparison of the average number of days for Temporal Min-Max vs. Binary representations for correct predictions.

for correct predictions.					
Problem 1 - Mortality					
Positive Label TS ⁺		Negative Label TS ⁻			
Temp CPM_1	Bin CPM ₂	Temp CNM ₁	Bin CNM ₂		
1259.6*	2599.1	2405.3*	1243.4		
1353.6	1413.3	1898.0*	1380.5		
1181.7*	1906.9	2608.1*	1193.3		
1595.1*	1680.8	1981.4*	1838.6		
Problem 2 – High Utilization					
1432.5*	1913.5	2070.2*	1555.0		
1468.2*	1754.1	1834.7*	1525.5		
1184.2*	2195.7	2362.4*	1213.2		
1579.9*	1669.6	1944.5*	1754.2		
	Positive TS Temp CPM ₁ 1259.6* 1353.6 1181.7* 1595.1* Proble: 1432.5* 1468.2* 1184.2*	Positive Label TS+ Temp Bin CPM ₁ CPM ₂ 1259.6* 2599.1 1353.6 1413.3 1181.7* 1906.9 1595.1* 1680.8 Problem 2 – High U 1432.5* 1913.5 1468.2* 1754.1 1184.2* 2195.7	Positive Label TS+ Negative TS Temp CPM₁ Bin CPM₂ Temp CNM₁ 1259.6* 2599.1 2405.3* 1353.6 1413.3 1898.0* 1181.7* 1906.9 2608.1* 1595.1* 1680.8 1981.4* Problem 2 - High Utilization 1432.5* 1913.5 2070.2* 1468.2* 1754.1 1834.7* 1184.2* 2195.7 2362.4*		

Table 6: Comparison of the average number of days for Temporal Min-Max vs. Binary representations for superior predictions.

Problem 1 - Mortality					
	Positive Label TS ⁺		Negative Label TS ⁻		
Alg	Temp SPM_1	Bin SPM ₂	Temp SNM ₁	Bin SNM ₂	
RF	1641.26*	1771.76	1920.35*	1816.88	
GB	1549.92*	1896.64	2004.06*	1699.10	
LR	1510.49*	1933.96	2103.39*	1643.55	
DT	1600.81*	1682.96	1977.14*	1842.69	
Problem 2 – High Utilization					
RF	1538.88*	1795.15	2048.76*	1644.65	
GB	1497.31*	1833.94	2055.30*	1587.85	
LR	1338.79*	2082.75	2188.95*	1459.63	
DT	1579.53*	1669.15	1942.51*	1755.21	

Another possible way to compare the models is to construct a model $C_{MI,M2}$ that predicts when one models is significantly better than the other, that is to classify SPM_1 and SNM_1 against SPM_2 and SNM_2 . Alternatively, SPM_1 against SPM_2 can be built if one is concerned only with positive cases. AROC > 0.5 for such a model indicates a pattern on cases for which one model dominates the other. Note such a model does not tell us if either of the models M_1 or M_2 are correct, but rather which is more likely to produce a better result for a given case. Typically, one should prefer $C_{MI,M2}$ to be an easy to interpret model such as logistic regression or decision tree so that conclusions can be drawn from the discovered patterns.

6 CONCLUSIONS

Model comparison is not a trivial task. Through comparisons, one can select the best model, but also gain useful insight into why specific models perform differently than others. It is clear that comparing models based on accuracy alone is not sufficient.

This position paper was not intended to present the best models or results for specific problems, nor to argue for the use of specific modeling methods. The two examples were used only for informative purposes and could be replaced with any other cases. The paper did also not mean to provide a full set of metrics and tasks to be performed in comparing models. Selection of the specific metrics should be done carefully to gain maximum insights into the application area. Instead, this paper was intended to contribute to an ongoing discussion on model evaluation and comparison. With ML field being dominated with statistical methods, researchers often assume that statistical model evaluation comparison are sufficient. This cannot be further from the truth, especially in the medical or health care fields in which every "test case" is a patient whose treatments and potentially life-altering decisions may be made based on predictions.

While presented in a different order, the presented methodology fits into a general framework used by the authors in which models are described by their inputs, models themselves and their outputs. The framework can be used to study model performance, explainability, fairness, and other factors that may ultimately lead to end users' trust and model adoption. It emphasizes the concept of *machine learning that makes sense*, in which the application of machine learning results in correctly constructed and evaluated models for which inputs mimic measurable real-world characteristics or modeled objects, and outputs directly correspond to outcomes of interest.

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