

UNDERSTANDING THE NATURE OF LEARNING:
ISSUES AND RESEARCH DIRECTIONS

by

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ABSTRACT

This chapter presents an overview of goals and directions in machine learning research, and is intended to serve as a conceptual road map to other chapters. It investigates intrinsic aspects of the learning process, classifies current lines of research, and presents the author's view of the relationship among *learning paradigms, strategies and orientations*.

1.1 Do We Need Learning Machines?

Artificial intelligence (AI) is now experiencing extraordinary growth and seeing its ideas and methods applied to many fields. Development of expert systems, practical implementations of natural language understanding systems, significant advances in computer vision and speech understanding, new insights into building powerful inference and qualitative reasoning systems are among its

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most visible and important successes. The rapid expansion of activities in AI leads us to believe that new successes are forthcoming.

In this context, it is important to ask what the limitations of the current methods are, and what new directions research in this field should take. One of the obvious limitations, and hence a direction for further research relates to *machine learning* - a field concerned with developing computational theories of learning and with constructing learning systems.

Except for experimental programs developed in the course of machine learning research, our current AI systems have rather limited learning abilities, or none at all. All of their knowledge must be programmed into them. When they contain an error, they cannot correct it on their own; they will repeat it endlessly, no matter how many times the procedure is executed. Neither can they improve gradually with experience, nor learn domain knowledge by experimentation. They cannot automatically generate their algorithms, formulate new abstractions, or develop new solutions by drawing analogies to old ones, or through discovery. Generally speaking, these systems lack the ability to draw *inductive inferences* from information given to them. One might say that almost all existing systems are *deductive*, as they are able to draw conclusions from knowledge incorporated in them, but cannot acquire or generate new knowledge on their own.

By contrast, when we look at human intelligence we see that among its most striking aspects is the ability to acquire new knowledge, to learn new skills, and to improve with practice. In time, use of these learning abilities can turn a young, inexperienced person into a journeyman engineer, educator, artist or physician. Our common perception is that a person who would repeat the same error again and again, could hardly be called intelligent. The ability to learn from error is considered fundamental to the individual, and to the society at large (Popper,

1959, 1963, 1981; Kuhn, 1970; Lakatos, 1970; Berkson and Wettersten, 1984; Hayes-Roth, 1983 - *Machine Learning I*, ch. 8).

Because learning ability seems to be so intimately entwined with intelligent behavior, the present situation has led some researchers to postulate that among new central goals for research in artificial intelligence should be to understand the nature of learning and to implement learning capabilities in machines (McCarthy, 1983; Schank, 1983). Overcoming the above-mentioned limitations sets an agenda for future research.

Questions then arise as to whether such a goal is achievable, and if so, whether it is desirable. Let us start with the question whether this goal is achievable. Answering it involves us immediately in questions of definition. Can we identify some general criteria such that, if satisfied by a machine, we would agree to call this machine a learning system?

As the machine learning research has shown, learning ability does not manifest itself as an all-or-nothing quality, but as a spectrum of information processing activities, ranging from the direct memorization of facts and a simple reorganization of information, to very intricate inferential processes leading to creation of new concepts and discovery of new knowledge. It always involves a change in a system, whether human or machine, that makes it better in some sense.

For now, let us put the question of definition aside (it is discussed in more detail in the next section), and observe that machine learning is experiencing a renaissance after its past steady but slow growth, and efforts to develop programs exhibiting some forms of learning have multiplied in recent years. This young field has already achieved a number of successes. A summary of some of these efforts is found in *Machine Learning: An Artificial Intelligence Approach* (Michalski, Carbonell and Mitchell, eds., 1983) - henceforth referred to as *Machine Learning I*.

The current book is a sequel, and reports some key subsequent efforts characteristic of the state-of-the-art in machine learning.

Based on the results achieved so far, it is clear that some rudimentary machine learning abilities are possible. Already there exist programs able to formulate new concepts and discover previously unknown regularities in data, develop decision rules that can outperform human rules, draw interesting analogies, automatically learn problem-solving heuristics or develop generalized plans for achieving a goal. Many of these programs are discussed in *Machine Learning I*. What is less clear is the level of progress that can be achieved in machine learning using conventional computer hardware and present programming methods. As always in science, such questions can only be answered by conducting further research and continuing to develop experimental learning systems.

New dimensions of research in machine learning will open with the development of *connection machines*, *fifth generation* computer systems, and other novel computer architectures, currently underway (Hillis, 1981; Kawanobe, 1984). For example, Hinton, Sejnowski and Ackley (1984) describe how learning may occur in *Boltzmann machines*. The knowledge acquired by such systems is represented by strengths of the connections between simple neuron-like elements. The research in this direction should address the problem of overcoming the limitations of early systems of this type, such as the *Perceptron* (Minsky and Papert, 1969). A new potential for research in machine learning also emerges in connection with the development of new programming systems, in particular logic programming, and its first embodiment in Prolog (Robinson, 1983).

Why is it desirable to develop learning machines? It appears, that the development of such systems is necessary to assure further progress in artificial intelligence, or closely related disciplines. This seems to be particularly true in areas such as expert systems or any large-scale knowledge-based systems, computer

vision and speech understanding, natural language understanding, intelligent tutoring systems and (truly) friendly man-machine interfaces. As more and more complex tasks are set for AI systems, the more and more knowledge must be represented in them. Such knowledge must encompass domain-specific facts and rules, common sense heuristics and constraints, as well as general concepts and theories about the world. The scope of knowledge in any system must be widened to avoid a common problem with the current systems, sometimes referred to as falling of the *knowledge cliff* (Feigenbaum, 1984) or *brittleness* (Holland, chapter 20; see also Larkin et al, 1985). The system performs well within the scope of knowledge provided to it, but any slight move outside of its narrow competence causes the performance to deteriorate completely.

Introducing all the required knowledge into any new system is a very complex, time consuming and error-prone process, requiring special expertise. For example, building an expert system involves a collaborative effort of highly trained experts - at least one *domain expert* and a *knowledge engineer* (Davis and Lenat, 1982; Hayes-Roth, Waterman and Lenat, 1983; Buchanan and Shortliffe, 1984). This task can be simplified by using machine learning techniques. Such techniques would enable a system to develop decision rules from examples of experts' decisions and through the automated analysis of facts in a database.

With the rapid increase in the amount of data and knowledge that the society generates, there is a growing need for not only storing, organizing and delivering this information, but also for using it in new creative ways. As knowledge can be viewed as *compressed information* (Rendell, 1983), we need machines that can compress databases and information systems into knowledge bases automatically via conceptual analysis of their contents. As envisioned by Michie (1982), "*the most technically gripping challenge, even if not immediately the most economically important, will be how to spread the computer wave from the front*

end of the scientific process, the telescopes, microscopes,...., spark chambers and the like, back to the recognition and reasoning processes by which the chaos of data is finally consolidated into orderly discovery."

This chapter's author may add, that in addition to the the computer's role as *scientist's* and *technologist's* intelligent assistants, we will also need intelligent *personal* assistants. Individuals in the expanding information society will need such assistants to cope with the overwhelming amounts of available information and the complexities of everyday decision making. To play the destined role, the function and knowledge of such assistants should be *dynamic*; these assistants should be able to adapt to the changing demands and be self-modifiable. That is, they should be able to learn.

A similar need for learning abilities exists in the areas of computer vision and speech understanding. To build a computer vision system, one has to incorporate into it a variety of vision-specific transformations, concepts of geometry, physical and functional descriptions of visual objects the system is to recognize, and related information (Winston et al, 1983; Winston, 1984). To "handcraft" all this information into a system is difficult. It would be much easier to teach the system by showing it examples of given concepts, and have it learn the appropriate generalizations and descriptions, just as we teach visual concepts to humans.

A system capable of understanding and interacting with humans in natural language has to be equipped with knowledge of syntactic properties of language (Marcus, 1980), as well as with many concepts and concept structures (such as, frames, scripts and schemata) capturing semantic and pragmatic aspects of the language (Winograd, 1981; Schank, 1982; see also chapters 19 and 21). One may estimate that in an advanced natural language understander, the number of such concepts and concept structures may easily reach tens of thousands, or more.

Programming all this knowledge into a computer is a monumental task. It is very desirable to simplify this task by employing a learning system. In addition, even if at some point all this knowledge were incorporated in a machine, a language understander would not work well for long without learning abilities. The meaning of human concepts is dynamic; it changes with time and adapts to new contexts and requirements. Novel concepts are continuously being created and developed, and some are being outgrown. Therefore, as in the cases above, we need a learning system capable of acquiring new concepts and concept structures by generalization from examples, or by analogy to prior knowledge. Such a system should be able to modify, specialize or generalize old concepts in a flexible fashion.

Intelligent tutoring systems must be able to present material at a level of difficulty and detail suited to the state of knowledge of the student. In order to do so, the system must know and follow the student's changing knowledge. A desirable way of acquiring this information is not by repeated direct testing but by learning from clues, behavior and implicit model of the student during tutorial sessions. Thus, learning abilities are required not only from the student but from the tutor as well (Sleeman and Brown, 1982; Sleeman, 1983 - *Machine Learning I*, ch. 16).

Through learning capabilities future computers should be able to acquire knowledge directly from documents and books, by conversing with humans, and by generalizing observations of their environment, which they make with their artificial senses. They should be capable of improving through practice and experience. It is possible that future machine learning systems will suffer little, if at all, from some human limitations, such as poor memory, distracted attention, low efficiency, and the difficulty of transferring acquired knowledge from one learner to another. Once one learning system is developed, a theoretically limitless

number of copies of it can be built, and then employed to learn new knowledge in diverse domains. In addition, any new knowledge acquired by a learning system can be copied to other systems rapidly and inexpensively (unlike human knowledge that must be painfully re-acquired by each new student).

Of course, we are still far away from such idealized vision, but it has now become conceivable that such learning systems might be developed in the future. It is then desirable to consider not only expected advantages, but also possible undesirable consequences. The last issue could be dismissed by saying that any new technology brings new opportunities for misuse, and this has never stopped us from developing it. Moreover, such aspects are usually considered an issue outside of the scientific or technical research. Yet we need to examine this particular issue carefully, for creation of machines able to self-acquire knowledge brings about new dimensions of complexity, and reflects on the way the field of machine learning should be developed.

The first dimension is predictive opacity of self-changing systems. To predict the behavior of machines that can learn inductively is considerably more difficult than to predict the behavior of machines without such an ability. The key idea behind learning machines is that they should be able to create knowledge that can surprize their human creators. This may cause unexpected difficulties, or even dangers, if someone should apply such a system to solve important problems, without understanding its limitations. In addition, the increased unpredictability of learning machines implies increased possibilities for their misuse.

Some experts argue that predicting behavior of complex computer systems is very difficult already. They look at the addition of learning capabilities to our computers as further amplification of these difficulties, but not as a quantum leap to a new state. Whether we see a leap, or merely an amplification of

unpredictability, a strong expectation is that potential benefits from this technology will amply compensate for such undesirable consequences. And with regard to the potential for its misuse, why not use these smart learning machines to "police" other machines, in order to prevent or combat attempted misuse?

In addition to the difficulty of predicting behavior of learning machines, there is another dimension for consideration, which stems from the very nature of any knowledge other than factual observation. As has been observed by Hume (see, e.g., 1888), and later by Popper (1979) and others, such knowledge is *inherently conjectural*. That is, any knowledge created by generalizing from specific observations, or by analogy to known facts, cannot in principle be proven correct, though it may be disproven.

This is because inductive inference is not *truth-preserving*, but only *falsity-preserving* (Michalski, 1983). To illustrate this point, consider a statement: "all scientists at the MIT's AI Laboratory are bright." A deductive conclusion from this statement can be that Roger Light, who works at the AI Laboratory, must be bright. If the original premise is true, then this deductive conclusion must be true also. An inductive inference from the initial premise might be: "all scientists at MIT are bright." In this case, even if the original premise were true, such inductive conclusion might not be. However, if the original premise is false, then this inductive conclusion must be false also. Thus, in contrast with a deductive system, correct inputs to an inductive system do not guarantee the correctness of the outputs. Moreover, for any given inputs, there is theoretically an infinite number of possible inductive conclusions. The ones we actually make reflect our preferences, assumptions and constraints that we use in formulating our generalizations (Medin, Wattenmaker and Michalski, 1985; Utgoff, chapter 5).

For the above reasons, in order to generate knowledge useful to us, it is important that learning machines be equipped with knowledge of all the relevant human constraints and assumptions. As it is unlikely that *all* subtle human and societal constraints and preferences will ever be made known to machines, there is the possibility that machine-generated knowledge will violate some of these constraints. A quote from Hofstadter (1980) is pertinent here: "*unless (the program) had an amazingly faithful replica of human body...it would probably have enormously different perspectives on what is important, what was interesting, etc.*" As the perception of what is important and what is interesting is a necessary component in guiding creation of new knowledge (Lenat, 1983), such differences are significant. Thus, when such knowledge created by a machine is used it may lead to solutions technically flawless but socially undesirable.

A related concern is that people may give too much credibility to the knowledge created by machines. This phenomenon has already been observed in related contexts, for example, in people unduly influenced by results of computer statistical analysis without clearly understanding its assumptions, or in people personifying a computer consultation system, such as Eliza (Weizenbaum, 1976). Also, while it may be known to scientists that inductively generated knowledge is inherently error-prone, this fact may be less obvious to non-experts.

An important implication of the above discussion is that any new knowledge generated by machines should be subjected to close *human scrutiny* before it is used. This suggests an important goal for research in machine learning: if people have to understand and validate machine generated knowledge, then machine learning systems should be equipped with adequate *explanation facilities*. Also, knowledge created by machines should be expressed in forms closely corresponding to human descriptions and mental models of this knowledge,

i.e., should satisfy what this author calls the *comprehensibility principle* (Michalski, 1983). When designing explanation capabilities for learning systems one should strive to facilitate not only human understanding of the surface results, but also of the underlying principles, assumptions and theories that lead to these results.

One may hypothesize that the existence of advanced learning machines, while eliminating the current *knowledge acquisition* bottleneck, could ultimately create the *knowledge ratification* bottleneck: so much new knowledge is generated by machines that it becomes difficult for human experts to test and approve it. Should this happen, future researchers will have an interesting problem to while away their idle hours. One may envision these researchers inventing sophisticated learning machines for designing experiments to test knowledge created by other sophisticated learning machines.

With these notes of concern mixed with arguments stressing the importance of machine learning, let us now look more closely at the intrinsic properties of the learning process.

1.2 What is Learning ?

As mentioned earlier, a common view holds that learning involves making changes in the system that will improve it in some way. In this description, the term "improve" needs more precision. Clearly, wine improves with time, but nobody would call such an improvement learning*. Simon (1983 - *Machine Learning I*, ch.2) gives a more precise characterization:

"Learning denotes changes in the system that are adaptive in the sense that they enable the system to do the same task or tasks drawn from the same population more effectively the next time."

* This example was suggested by Steve Tanimoto from the University of Washington in Seattle.

The requirement that a system improve performance for learning to take place is widely accepted. There are, however, activities that can be categorized as learning, in which the *improvement criterion* is difficult to apply (a discussion of this problem follows). Minsky (1985) in his insightful theory of thinking, *the Society of Mind*, replaces this criterion with a more general one requiring that changes are merely useful:

"Learning is making useful changes in our minds" .

He subsequently observes that such a definition is too broad to be of any use. Let us then approach the problem of capturing the fundamental aspects of learning in another way. It may be observed that learning is often equated simply with acquiring *new* knowledge, as in the statement: "As the satellite burned in the atmosphere, the Spacelab astronaut *learned* that the satellite had an auxiliary antenna". In this case, the astronaut simply acquired a piece of information, but this will never improve his performance with *this* satellite.

The *knowledge acquisition* aspect of learning seems to be the *essence* of most of the learning acts. Those acts where it appears to play only a small role are cases of what is usually termed *skill acquisition*. The latter refers to gradual improvement of motor or cognitive skills through repeated effort, sometimes involving little or no conscious thought (Carbonell, Michalski and Mitchell, 1983 - *Machine Learning I*, ch.1). In this discussion we will concentrate, however, on the knowledge acquisition aspect of learning, a theme which recurs throughout the book.

In order to acquire knowledge of anything, one, obviously, has to represent this knowledge in some form, whether as declarative statements, as procedures, as a mixture of the two, or as something else (McCarthy, 1968). This fact and the considerations above lead us to the following characterization of learning:

Learning is constructing or modifying representations of what is being experienced.

The concept of *experience* includes here any sensory stimuli, as well as internal *Gedanken* processes. These stimuli and internal processes are the vehicle through which the learning system perceives the reality that it is trying to represent. The internal thought processes can themselves be a subject of learning.

Thus, from the above view, the central aspect of learning is the process of constructing a representation of some reality, rather than improvement of performance. The performance improvement is considered to be a consequence and often the purpose of building the representation, but it can be asserted only in the context of the learner's goals. Because most learning acts indeed involve improvement of performance, and because it is easier to measure performance than to read minds, naturally we link the two. Yet, performance improvement does not seem to be an invariable condition for every act of learning. There are situations in which it does not appear to be of primary relevance, as in learning to appreciate beauty. There are also situations in which it may even be misleading. The latter situations occur when it is difficult to accurately assess the learner's goal. For example, a worker in a labor camp may want to learn how to do less and appear to do more, yet keeps this goal secret. From the viewpoint of an external observer, this worker will appear not to be learning, as his performance will be decreasing with practice. Thus it seems clear that to determine learning by measuring performance may not be possible without knowing the goals of the learner.

Three dimensions seem to be particularly important for evaluating the constructed representations: *validity*, *effectiveness* and *abstraction level*. Validity (or truthfulness) refers to the degree of accuracy with which the representation fits the reality. It characterizes the precision of the mapping between the reality and the representation. The second criterion, effectiveness, attempts to capture the performance aspect of learning. It characterizes the usefulness of the representation for achieving a given purpose or goal. The more effective the representation, the better the performance of the system. Thus this criterion is central for tasks in which performance is of primary concern. The third criterion, abstraction level, reflects the scope, detail, and precision of concepts used in the description. It defines the *explanatory* power of the representation. These three dimensions together determine what may be called the *quality* of learning.

The representations can be in the form of symbolic descriptions, algorithms, simulation models, control procedures, plans, images, or general formal theories. If one stretches the concept of representation to include physical or physiological imprints occurring in the nervous system when one is acquiring a skill, the above view of learning seems to also cover skill acquisition.

From this viewpoint, a fundamental problem in any research on machine learning concerns the form and method used to represent and modify the knowledge or the skill being acquired. With regard to the question of modifying knowledge, it is important to identify the components and the properties of the representation which are modifiable by the system and which are not.

In the taxonomy of machine learning research given in (Carbonell, Michalski and Mitchell, 1983 - *Machine Learning I*, ch.1), three criteria were indicated as especially useful for classifying and comparing machine learning investigations: *learning strategy*, *knowledge representation* used, and the *application domain*. The learning strategy refers to the type of inference employed by the

system during learning. Some additional ideas reflecting recent progress on this topic are presented in section 1.4. The criteria of knowledge representation and the application domain were well covered in the above mentioned reference, and will be omitted here. Instead, we will discuss in some detail two other classification criteria, *research paradigms* (next section), and *learning orientations* (section 1.5). The research paradigm criterion refers here to the approach taken to construct a system, and the learning orientation refers to the scope and the subject of study.

1.3 Research Paradigms

Since the inception of machine learning in the fifties, research efforts have placed the emphasis at different times on different approaches and goals. One can distinguish three major research paradigms or approaches in this area: *neural modeling* and *decision theoretic techniques*, *symbolic concept acquisition*, and *knowledge-intensive domain-specific learning*. These research approaches differ chiefly in the amounts of *a priori* knowledge the learning system has built-in and in the way knowledge is *represented* and *modified* in the system.

The neural modeling approach strives for building general purpose learning systems that start with little initial knowledge. Such systems are usually referred to as *neural nets* or *self-organizing* systems. A system of this type consists of a network of interconnected elements, typically neuron-like, which perform some simple logical function, for example, a threshold logic function. Such a system learns by incrementally modifying the *connection strengths* between the elements, usually by changing weights associated with these connections. The system's initial knowledge is provided by the choice of the input elements that represent selected attributes of objects under study, and by the structure and initial strength of the connections in the network. This can be a random structure, one prearranged by the designer,

or a mixture of the two. Such learning systems include the *Perceptron* (Rosenblatt, 1958), *Pandemonium* (Selfridge, 1959), and any learning machine using *discriminant functions* (Nilsson, 1965). More recent examples stemming from this paradigm are various adaptive control systems (Tsyppkin, 1972). Research in this area has led to the *decision-theoretic approach* in pattern recognition. A related to this approach is research on *evolutionary learning* (Fogel, Owens and Walsh, 1966; Conrad, 1983), and *genetic algorithms* (Holland, 1975; see also chapter 20). As mentioned earlier, there is a resurgence of interest in this learning paradigm with the recent efforts to develop *connection machines* (Hinton, Sejnowski and Ackley, 1984).

Low levels of *a priori* built-in knowledge and use of continuously changeable parameters to achieve learning are characteristic features of systems built under this paradigm. A related feature is the numerical character of learning methods and algorithms. This stands in contrast with the next two paradigms, where the main stress is on creating and manipulating complex symbolic structures during the process of learning.

In *symbolic concept acquisition* (SCA), the system learns by constructing a symbolic representation of a given set of concepts through the analysis of examples and counter-examples of these concepts. The representation may be in the form of a logical expression, a decision tree, production rules, or a semantic network. Some of the systems developed under this paradigm have multi-purpose applicability and have demonstrated practical usefulness. Examples of such systems are Winston's Arch program (Winston, 1975), the AQVAL program (Michalski, 1975) and ID3 (Quinlan, 1979). In this paradigm, the attributes or predicates relevant to the concept are provided to the system by the teacher.

In *knowledge-intensive domain-specific learning* (KDL), the system contains numerous predefined concepts, knowledge structures, domain constraints, heuristic rules and built-in transformations relevant to the specific domain for which the

system is built. Not all the relevant attributes or concepts are provided initially; the system is expected to derive new ones in the process of learning (this author refers to such a process as *constructive induction*). Thus, the main differences between the KDL and SCA paradigms are in the amount and the kind of background knowledge supplied to the system. Learning systems based on this approach are typically developed for a specific domain, and cannot be directly used in another domain. The research in this paradigm have explored not only the strategy of *learning from examples*, but also strategies such as *learning by analogy*, and *learning by observation and discovery* (see next section). Examples of systems based on this approach are Meta-DENDRAL (Buchanan, 1978) and AM (Lenat, 1983).

Many systems developed in the past represent a certain mixture of the above-mentioned approaches. An interesting combination of the SCA and KDL approaches represents a system based on the idea of an *exchangeable knowledge module*. Such a system combines the general-purpose learning mechanisms with the built-in facilities for defining and using domain-specific knowledge. When such a system is applied to a given problem, the domain-specific knowledge is supplied to it by the teacher via system's knowledge representation facilities. By separating general inference capabilities from the domain-specific knowledge, such a learning system can be applied to a spectrum of different domains, and still take advantage of domain-specific knowledge in the process of learning. Such a philosophy underlies the INDUCE system, which learns structural descriptions of objects from examples (Michalski, 1980). Winston's program for learning by analogy is another example (Winston, 1982). Also, the LEX system, for acquiring and refining problem-solving heuristics (Mitchell, Utgoff and Banerji, 1983), and the Eurisko program for discovering new heuristics (Lenat, 1983) can be characterized in such

terms. Chapter 14 (Carbonell) describes such an approach in the context of *derivational analogy*.

For an historical review of these three research paradigms the reader is referred to Chapter 1 in *Machine Learning I*. A sample of contemporary research on self-organizing systems is found in Caianiello and Musso (1984). A recent review of approaches to machine learning has been made by Langley and Carbonell (1984). The primary concern of this book is symbolic concept acquisition and knowledge-intensive domain-specific learning.

1.4 Learning Strategies

In every learning situation, the learner transforms information provided by a teacher (or environment) into some new form in which it is stored for future use. The nature of this transformation determines the type of learning strategy used. Several basic strategies have been distinguished: rote learning, learning by instruction, learning by deduction, learning by analogy and learning by induction. The latter subdivides into learning from examples and learning by observation and discovery. These strategies are ordered by the increasing complexity of the transformation (inference) from the information initially provided to the knowledge ultimately acquired. Their order thus reflects the increasing effort on the part of the student, and correspondingly decreasing effort on the part of the teacher. Distinguishing these strategies is useful for tutorial purposes, and for the design of learning systems as well. In any act of human learning, a mixture of these strategies is usually involved. Though most of current systems focus on a single learning strategy, one may expect that machine learning research will give an increasing attention to multi-strategy systems. Chapter one of *Machine Learning I* describes these learning strategies in detail. Because of their importance to this

book, and because of some changes in their classification brought about by recent research, we will briefly review them here.

In *rote learning* there is basically no transformation; the information from the teacher is more or less directly accepted and memorized by the learner. A major concern here is how to index the stored knowledge for future retrieval. In *learning by instruction* (or *learning by being told*), the basic transformations performed by a learner are *selection* and *reformulation* (mainly at a syntactic level) of information provided by the teacher. In *deductive learning*, the learner draws deductive, truth-preserving inferences from the knowledge given, and stores useful conclusions (this strategy was identified as a separate category only recently (Michalski, 1983, 1985)). Deductive learning includes knowledge reformulation, knowledge compilation, creating macrooperators, caching, chunking, some forms of operationalization, and other truth-preserving operations (see glossary).

If the transformation process involves generalization of information and evaluation of the result, that is, inductive inference, then we have *inductive learning*. *Learning by analogy* is deductive and inductive learning combined. Here descriptions from different domains are matched to determine a common substructure. This common substructure serves as the basis for analogical mapping. Finding the common substructure involves inductive inference, while performing analogical mapping is a form of deduction. *Learning by reminding* described by Schank (1982) can be viewed as a form of learning by analogy. Learning by analogy is discussed in chapters 13 (Burstein), 14 (Carbonell) and 15 (Dershowitz).

Inductive learning can be subdivided into learning from examples, and learning by observation and discovery. In *learning from examples* (also called *concept acquisition*), the task is to determine a generalization explaining all positive examples and excluding all negative examples of the target concept. The examples are provided by a source of information, which can be a teacher who knows the

concept, or the environment on which the student performs experiments and from which it receives feedback. In the latter case we have *learning by experimentation* (this includes *learning by doing* and *learning by problem solving*). The *stimulus-response* learning can also be classified as a form of learning from examples.

Recent research has revealed two interesting subdivisions within this form of learning: *instance-to-class* and *part-to-whole* generalization. In *instance-to-class* generalization, the system is given independent instances (examples) of some class of objects, and the goal is to induce a general description of the class. Most research done on learning from examples has been concerned with such *instance-to-class* generalization. The objects could be structured blocks, geometrical shapes, descriptions of diseases, stories, problem solutions, control operators, etc. Various aspects of this problem are discussed in: Chapter 3 (Winston), Chapter 5 (Utgoff), Chapter 6 (Quinlan), Chapter 7 (Sammut and Banerji), Chapter 8 (Lebowitz) and Chapter 9 (Kodratoff and Ganascia). For a review of earlier methods for such generalization see (Dietterich and Michalski, 1983; Cohen and Feigenbaum (Eds.), 1981).

In *part-to-whole* generalization, given selected parts of an object (of a scene, a situation, a process), the task is to hypothesize a description of the whole object. For example, given a collection of snapshots of selected parts of a room, reconstruct the total view of that room. Another example of this form of generalization requires the system to determine a rule (a theory) characterizing a sequence of objects or a process, from seeing only a part of this sequence or process. This type of problem is considered in Chapter 4 (Dietterich and Michalski). A closely related research concerns the *qualitative process prediction* (Michalski, Ko and Chen, 1985).

In *learning by observation and discovery* (also called *descriptive generalization*), one searches, without the help of a teacher, for regularities and

general rules explaining all or at least most observations. This form of learning includes *conceptual clustering* (forming object classes describable by simple concepts), constructing classifications, fitting equations to data, discovering laws explaining a set of observations, and formulating theories accounting for the behavior of various systems. *Genetic algorithms* (Holland, chapter 20), and *empirical prediction algorithms* (Zagoruiko, 1975) can be viewed as variants of this learning strategy. Various aspects of this strategy are discussed in Chapter 16 (Langley et al.), 17 (Stepp and Michalski), 18 (Amarel) and 19 (DeJong).

The primary focus of this book is on learning by induction and analogy. Therefore, before moving to the next topic, it may be useful to make a few additional comments about inductive inference which is at the heart of these strategies. Inductive inference starts with a set of facts (observations), and optionally with an *a priori* hypothesis about these facts, and produces a preferred generalization explaining these facts. As mentioned before, it is a falsity-preserving inference accomplished by the application of *generalization inference rules* (Michalski, 1983). As noted by Popper (1972) and others, "pure" induction, that is, direct inference from facts to theories without any *interpretive (explanatory)* concepts, is impossible. These concepts are needed to describe the observations, and are part of the learner's *background knowledge*. This background knowledge is a necessary component of any inductive process. It includes also goals of learning, domain-specific constraints, causal relationships, heuristics and biases that guide the generalization process, and the criteria for evaluating competing hypotheses.

One can distinguish two techniques for guiding and constraining generalization: the similarity-based and the constraint-based techniques. The *similarity-based* technique explores *inter-example* relationships, that is, it examines

the examples and counter-examples of a concept in order to create a concept description. It searches for features shared among facts or examples in the same class, looks for common causes and explanations why different examples belong to the same class. It generalizes over the differences between examples either by ignoring the differing features, or by formulating concepts that encompass the differences. Some early learning methods using this technique are reviewed by Dietterich and Michalski in chapter 3 of *Machine Learning I*.

The *constraint-based* technique exploits the *intra-example* relationships, which constrain the interpretive or explanatory concepts applied to one or more facts or examples. Any generalization of these facts or examples must satisfy these constraints. For example, when generalizing the fact that "a box is on the table," one should satisfy the constraint that whatever is on the table cannot be so heavy that it would break the table, or so large that it could not be placed on the table.

A variant of this technique is described by Andreae (1984), who uses the concept of a *justification* for a hypothesis. Another variant is called by some authors an *explanation-based* generalization, in order to stress the role of explanatory knowledge used by the method (this is probably not the most informative term, because any type of inductive learning, by definition, involves searching for an explanation of the facts provided). DeJong, in Chapter 19, discusses a method implementing such a technique in the context of story understanding. The similarity-based and constraint-based techniques are complementary, and can be used simultaneously in learning systems.

1.5 Learning Orientations

Sections 1.3 and 1.4 discussed two important classifying criteria for machine learning research respectively: *learning paradigms* and *learning strategies*. To recapitulate, the first criterion concerns the type of knowledge represented and

manipulated in the system, while the second criterion deals with the type of inference performed on the knowledge. This section will briefly discuss one more classifying criterion, the *research orientation*, which concerns the scope and subject of study. To draw an analogy, a *paradigm* corresponds to one's point of departure and the terrain through which one travels, a *strategy* specifies the means of locomotion, and an *orientation* indicates the destination.

As described in Chapter 1 of *Machine Learning I*, research in machine learning encompasses three interconnected orientations:

- A. Theoretical analysis and development of general learning algorithms;
- B. The development of computational models of human learning processes;
- C. Task-oriented studies concerned with building learning systems for specific applications (called also an engineering orientation).

The first orientation investigates theoretical learning tasks, or simplified practical ones, and tries to develop algorithms that accomplish these tasks independent of application. There is no restriction on the type of algorithm developed. The algorithm need not be similar to that which a human might use to perform the given task. As a variation, some authors postulate that at least the knowledge structures generated as an end result of learning should be similar to those a human being might create; the process of their creation can be different (Michalski, 1983). This research orientation strives to chart the theoretical space of possible learning algorithms. Chapters 3 (Winston), 5 (Utgoff), 7 (Sammut and Banerji) and 9 (Kodratoff and Ganascia) represent a sample of work representative of this orientation.

The second orientation, also called *cognitive modeling*, takes human learning as its focus, and tries to develop computational theories and experimental

models of human learning. This research will likely have important influence on human education, as well as on the techniques of implementing machine learning systems. Chapters 10 (Rosenbloom and Newell), 11 (Anderson) and 14 (Carbonell) are characteristic of this orientation.

Finally, the third orientation undertakes specific practical learning tasks and tries to develop engineering systems capable of performing these tasks. An example here would be a program that learns to recognize dangerous conditions for aircraft in flight. Such efforts usually have to address a host of other problems not directly related to learning, such as the appropriate interpretation of the input signals or the development of problem-specific transformations of the data. This orientation readily adopts any useful ideas from the other two orientations. Often, after a solution to a specific problem is found, it is generalized to a method for solving a class of similar problems. An example of such research is described by Dietterich and Michalski in Chapter 4.

The above three research orientations make up a trichotomy of mutually dependent and supportive efforts that fuel the machinery of learning research. Such a trichotomy has come to pervade the whole of artificial intelligence.

1.6 Reader's Guide to this Book

As indicated in the sections above, this book is concerned with the SCA (symbolic concept acquisition) and the KDL (knowledge-intensive domain-specific learning) paradigms, and concentrates on inductive and analogical learning strategies. Both major types of inductive learning, that is, learning from examples and learning by observation and discovery, are represented. The chapters are grouped into six parts reflecting the major learning strategy employed or the research orientation of the work.

Part One provides an *introduction* and *discussion* of general issues in the field of machine learning. After this overview, **Chapter 2** presents views from several researchers on important problems in this field for the decade of the 80s. These topics emerged from a panel discussion held at the Second International Machine Learning Workshop, University of Illinois, 1983 (the proceedings are in Michalski (Ed.), 1983).

Part Two describes a selection of results on *learning from examples*. In **Chapter 3**, Winston integrates ideas about several interrelated topics: learning from precedents and exercises, the use of *near misses* in learning, generalizing *if-then* rules and employing *unless* conditions to prevent an incorrect rule application. The role of an *unless* condition is to block a given *if-then* rule whenever facts at hand satisfy this condition. Such a condition facilitates an incremental improvement of rules.

In **Chapter 4**, Dietterich and Michalski present a theoretical framework and methodology for *part-to-whole* generalization. They describe a general method utilizing several rule models for discovering a rule that characterizes a sequence of objects and predicts a plausible sequence continuation. Each object in the sequence is described by discrete attributes, which are either given *a priori*, or derived by applying various inference rules and sequence transformations.

Utgoff in **Chapter 5** investigates the role of *bias* or *preference criterion* in determining a plausible hypothesis in inductive learning. He presents a methodology and a program STABB for shifting bias in the course of learning from examples.

In **Chapter 6**, Quinlan examines the effect of noise in training examples on the discovery of classification rules and their accuracy. He makes several interesting conjectures about how to formulate the learning task when training examples are expected to contain noise.

Next, in Chapter 7, Sammut and Banerji investigate the role of previously learned concepts in learning new ones, and the problem of inductive learning with an *active* learner. Such a learner is not just passively accepting examples from a teacher, but is also generating examples on its own and asking the teacher whether they represent the concept being learned.

In Chapter 8, Lebowitz discusses a somewhat related problem. He explores the use of concepts stored in the memory for generalizing complex structural descriptions. His *generalization-based memory* method determines what concepts to learn, and formulates definitions of the concepts learned. The ideas are exemplified by two programs, one for concept evaluation, and the second for generalization of complex structural descriptions.

Next, in Chapter 9, Kodratoff and Ganascia discuss various theoretical aspects of the generalization process. They show how generalization is accomplished by creating links among training examples. These links are represented as variable bindings.

Part Three takes up *cognitive aspects of learning*. In Chapter 10, Rosenbloom and Newell present ideas about modeling processes that underlay improvement of performance by practice. Their model of practice is based on the concept of *chunking*, that is grouping subgoals into higher goals. They show that this model explains the known *power law* of human practice.

Next, in Chapter 11, Anderson discusses learning mechanisms involved in *knowledge compilation*, that is in the process by which subjects go from declarative representation of a skill to a procedural representation. He shows how mechanisms of *composition* (collapsing multiple productions into a single production), and *proceduralization* (building into productions information that resides in declarative

form in the long-term memory) can simulate the initial stages of skill acquisition in the domain of learning how to program.

In Chapter 12, Forbus and Gentner present their work on a computational model of human learning of physical domains. They use *qualitative process theory* to model human physical knowledge and *structure-mapping theory*, which characterizes analogy and other comparisons, to describe processes of changing knowledge representations.

Part Four focuses on the topic of *learning by analogy*. Burstein, in Chapter 13, presents a model of learning by analogical reasoning. He describes it in the context of acquiring semantics of assignment statements in the BASIC programming language. According to his model, the use of analogies to learn concepts in a new domain depends strongly on causal abstractions previously formed in a familiar domain. These analogies are extended incrementally to handle related situations.

In Chapter 14, Carbonell presents his theory of *derivational analogy*, and its implications for case-based reasoning and expertise acquisition. In essence, the derivation of solutions to related problems is replayed and modified to solve newer and increasingly more complex problems. The method is proposed as a means of automating knowledge and skill acquisition for expert systems.

Dershowitz, in Chapter 15, focuses on analogy as a tool for automatic programming. He shows how analogies between program specifications (as well as between their derivations) can be used to debug a program, or to modify an existing program to perform a new task. These analogies can also be used to derive an abstract schema of a set of programs, and to instantiate a schema in order to yield a particular program.

Part Five covers *learning by observation and discovery*. In Chapter 16, Langley, Zytkow, Simon and Bradshaw describe four systems addressing different

aspects of scientific discovery. BACON.6 formulates empirical laws characterizing any numerical observational data. GLAUBER takes on discovery of qualitative laws of chemical reactions. STAHL undertakes the problem of determining components of substances involved in such reactions. Finally, DALTON focuses on the formulation of structural models for these reactions.

In Chapter 17, Stepp and Michalski report on their recent work on *conceptual clustering*, that is creating a classification of observations by identifying subclasses that correspond to simple concepts. Unlike previous work on generating goal-free classifications of unstructured objects, the new research takes on constructing goal-oriented classifications of structured objects. They describe and illustrate by examples how a learner's concepts and inference rules are used in constructing such purposive classifications.

In Chapter 18, Amarel discusses problems of theory formation in the context of program synthesis. He illustrates his method and ideas by a problem of inferring a program from input-output data associations in the domain of partially ordered structures. His method emphasizes the role of algebraic and geometric models, and the importance of shifting problem representations in the program synthesis task.

Taking a different tack, DeJong in Chapter 19 discusses a method of learning from observation, which exploits the inner constraints among explanatory concepts in the system's background knowledge, to guide the process of generalization from a single example. His examples are stories about people's problem-solving behavior. This knowledge-based generalization process is used to propose new schemata.

Part Six explores some general aspects of learning. In Chapter 20, Holland discusses general-purpose learning algorithms based on a parallel rule-based system architecture. He advances the theme that inductive processes in such rule-based

systems are a way of overcoming the *brittleness* of current AI systems, which is due to the narrow scope of their domain-specific knowledge.

In Chapter 21, Berwick explores the issues of general constraints underlying processes of natural language acquisition. He discusses the relative importance of general, domain independent learning principles versus domain specific learning.

Finally, in Chapter 22, Silver describes how a method, called *precondition analysis*, can learn strategies for problem-solving. He illustrates his method by examples in the domain of algebraic equations.

The book concludes with a bibliography of research in machine learning done since 1980, with a few major landmarks representing earlier research. (A comprehensive bibliography of previous research in this field can be found in *Machine Learning I*.) The bibliography is indexed by underlying learning strategy, domain of application and research methodology. An updated glossary of terms in machine learning is provided, as well as a bibliographical note about each author.

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