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**A Preliminary Experimental Application of
Learnable Evolution Model and Evolutionary Algorithms
to Parameter Estimation in
Non-linear Digital Signal Filter Design**

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ABSTRACT

This paper describes an application of LEM1, a preliminary implementation of Learnable Evolution Model (LEM), and two evolutionary algorithms, GA1 and GA2, to parameter estimation in non-linear digital signal filter design. LEM1 alternates between two modes of operation: Machine Learning mode, which employs AQ-18 rule learning system, and Darwinian Evolution mode, which employs evolutionary algorithm GA2. Machine Learning mode generates hypotheses as to what type of individuals in a population represent high fitness solutions. These hypotheses, expressed in the form of attributional rules, are used to generate new populations of solutions. When the top fitness of a population has not improved sufficiently during one mode, LEM1 switches to another mode. LEM1 alternates between the two modes until a global termination condition is satisfied. In the experiments, LEM-1 significantly outperformed evolutionary algorithms GA1 and GA2.

Keywords: Evolutionary computation, Learnable Evolution Model, Evolutionary algorithms, Function Optimization, Symbolic Learning, AQ18, Digital Filters.

1 INTRODUCTION

Parameter estimation problems solved by steepest descent methods require a computation of the gradient of the error surface. Computation of the gradient of a multi-modal error surface can, however, be extremely computationally intensive for problems with many variables. For some spaces derivatives are not defined and gradients cannot be computed at all. To solve such complex parameter estimation problems evolutionary algorithms can be used (Yao, Sethares, 1994). Unlike the steepest-descent approach, evolutionary algorithms do not require the computation of the gradient of the error surface. In addition, due to their inherent stochastic nature, evolutionary algorithms are less susceptible to settling on a local minimum.

A major difficulty with evolutionary algorithms is that they are computationally inefficient because they conduct a stochastic trial and error process. A new approach is offered by Learnable Evolution Model (LEM), which was recently introduced by Michalski (1998, 1999). LEM combines two modes of operation: Machine Learning mode and Darwinian Evolution mode.

In Machine Learning mode, LEM employs a learning system that generates hypotheses that differentiate high performing individuals from low performing individuals in the population. The first system implementing the LEM approach, LEM1, applied the AQ15c symbolic learning method in Machine Learning mode and canonical evolutionary algorithm GA2 in Darwinian Evolution mode (Michalski, 1973; Michalski et al., 86; Wnek et al, 1996).

LEM1 and two evolutionary computation algorithms, GA1 and GA2, were applied to a set of function optimization problems based on the (De Jong, 1975) and their inverse (Michalski, 1998, Michalski and Zhang, 1999; Michalski, 1999). In these experiments, LEM1 significantly outperformed GA1 and GA2.

This paper describes an improved version of LEM1 (which uses AQ18 rather than AQ15c learning program; see Michalski and Kaufman, 1999), and applies it to a different class problems, specifically, to parameter estimation in non-linear digital filter design.

2 BRIEF DESCRIPTION OF LEM1, GA1 AND GA2

The LEM method works by alternating between Darwinian Learning mode and Machine

Learning mode (the duoLEM version), or works solely in Machine Learning mode (the uniLEM version). In this study we experimented with duoLEM version. In this version, a switch from one mode to another is made when the fitness of the population is not improving sufficiently for a certain number of generations.

The LEM method is defined as follows (Michalski, 1998, 1999):

1. Randomly, or according to certain prior rules reflecting domain knowledge, generate the starting population of solutions (in the case of parameter estimation problems, this population is a starting set of parameter values).
2. Execute *Darwinian Evolution mode* (using some form of selection, crossover and mutation operators), as long as the best solution in a sequence of iterations (defined by parameter *dar-probe*) is better by the best solution found in previous generations (by the amount defined by parameter *dar-threshold*).
3. Execute *Machine Learning mode* (using a machine learning method)
 - (a) Determine HIGH-performance solutions (H-group) and LOW-performance solutions (L-group) in the current population, according to the fitness function defined for a given task or problem.
 - (b) Apply machine learning method for characterizing differences between H-group and L-group.
 - (c) Generate a new population of solutions by replacing not-H-group individuals by those satisfying the learned description of H-group solutions; the selection of new solutions among those satisfying the description is random or according to the predefined selection rules (a simple variant of the LEM method).
 - (d) Go to step (a), and then continue Machine Learning mode as long as the best solution in a sequence of iterations is better than the previously found best solution.
4. Switch to (2), and repeat the process. Continue switching between mode (2) and (3) until the *termination condition* is met (the generated solution satisfactory, or the allocated computation resources are exhausted).

In LEM1, the step 3(b) is executed by supplying H-group and L-group to an AQ-type learning system. In our experiments, we used AQ18 system (Kaufman and Michalski, 1999), which hypothesized attributional descriptions of high performing individuals. These descriptions were used to generate a new population of individuals for the next evolutionary computation step. GA1 and GA2, obtained from Ken De Jong, employ mutation and standard selection operators to alter populations. GA2 also has a uniform crossover operator, so a child has an equal probability of receiving a gene value from each parent. LEM1 uses GA2 during its evolutionary algorithm mode, employing mutation, standard selection, and crossover. These algorithms do not use elitism.

3 PROBLEM STATEMENT

We applied the LEM1 system to problems of identifying parameters in digital filters. Fitness functions were defined on the basis of equations specifying linear and non-linear filters. These equations are described in the paper “Nonlinear Parameter Estimation via the Genetic Algorithm” (Yao and Sethares, 1994):

Linear filter:

$$y(k) = -0.3y(k-1) + 0.4y(k-2) + 1.25u(k-1) - 2.5u(k-2) + n(k)$$

Non-linear filter:

$$y(k) = \left[\frac{3 - 0.3y(k-1)u(k-2)}{5 + 0.4y(k-2)u^2(k-1)} \right]^2 + (1.25u^2(k-1) - 2.5u^2(k)) \ln(|1.25u^2(k-2) - 2.5u^2(k)|) + n(k)$$

where:

k – is the sample index (or time)

$n()$ – is a noise component ranging from -.25 to .25

$u()$ – represents an inserted function (sin, step, etc.)

To apply the evolutionary computation approach, coefficients -0.3, 0.4, 1.25, and -2.5 in both equations were replaced by four real-valued variables. Values of these variables constitute “genes”; vectors of these values comprise “chromosomes,” or individuals of a population. The problem is to determine coefficients of these equations, given a list of $y(k)$ values for a number of k values.

The evolutionary process generates a population of individuals. The best individual in the population of a given generation is viewed as a current solution of the problem. When substituted into equation 2, a result is obtained that is compared with the correct value, computed from the equation with known coefficients. The fitness of an individual is inversely proportional to the mean-square error between the obtained result and correct value. Thus, the individual that yields the lowest error has the highest fitness. The goal of this process is to find an individual that minimizes the mean-square error.

The parameters of the evolutionary algorithms used were as follows, for both the linear and non-linear equations:

<i>Gene representation</i>	<i>Domain</i>
Number of genes per individual	4
Gene landscape (constraint on range)	-30 to 30
Number of individuals per generation	60
Mutation Rate	25%
Maximum number of births	100,000
Maximum number of generations	1500

4 EXPERIMENTS

We ran LEM1, GA1, and GA2 for the linear and nonlinear filters with three different input data. As done by Yao and Sethares (1994), we also used a uniformly distributed random input over the interval $(-2.5, 2.5)$. In addition to this random input, we also used a unit step function $2.5u(k)$ and a sine wave $2.5\sin(\pi/10)$ to see how the algorithms compared work with different types of inputs.

To represent all three types of inputs, random, sine, and step function, we quantized them into 200 sample input sequences. These input sequences were applied to the filter equations to compute the filter output. This output was then compared at each of 200 points with the output from the equations with the known correct coefficients. The evolutionary process ran for 1500 generations. At each generation, the fitness of each individual in a population is the reciprocal of

the sum of the mean-square error for the output sequence generated for a given input sequence. Thus, the fitness of an individual is defined by the equation (Yao and Sethares, 1994):

$$Fitness = \frac{1}{MeanSquareError} = \frac{200 samples}{\sum_{200 sample window} (individual - known)^2}$$

The mean-square difference between the correct and output values obtained at the end of the evolutionary process constitutes the error of the parameter estimation for this process.

In the case of the linear filter parameter estimation problem, LEM1 outperformed GA1 and GA2. All algorithms, however, converged very rapidly, and we do not present these results here. With regard to non-linear filter parameter estimation problem, we ran LEM1, GA1, GA2 ten times for each type of input (sine, step, and uniform random noise). Each run started with a different randomly generated population. We observed that the results were varying significantly with the starting population. Runs that produced large errors dominated solutions that produced small errors. Therefore, we found it more representative to select the best runs for each type of input and each algorithm.

These runs are characterized by curves that represent the relationship between the mean-square error and the number of generations (learning curves). These learning curves are presented in Figures 1 to 9 for each type of input (sine, random, step) and for each algorithm (GA1, GA2, and LEM1). Figures 1-3 present results with a sine wave input, Figures 4-6 show results with unit step input, Figures 7-9 show results with uniform noise input.

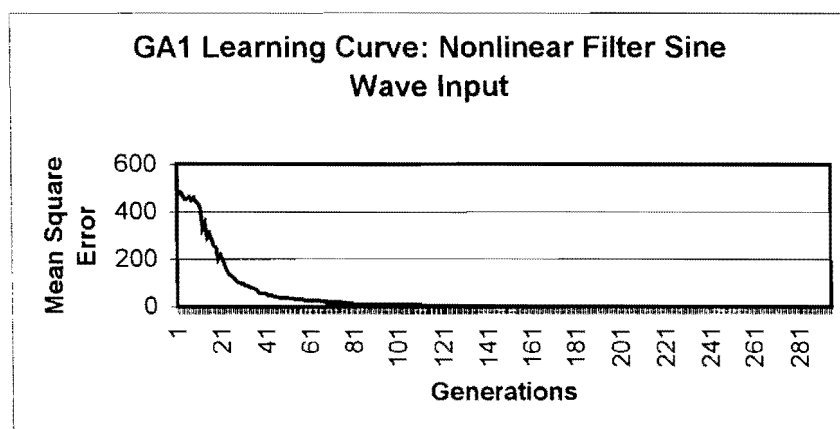


Figure 1: GA1 learning curve, nonlinear filter, sine wave input.

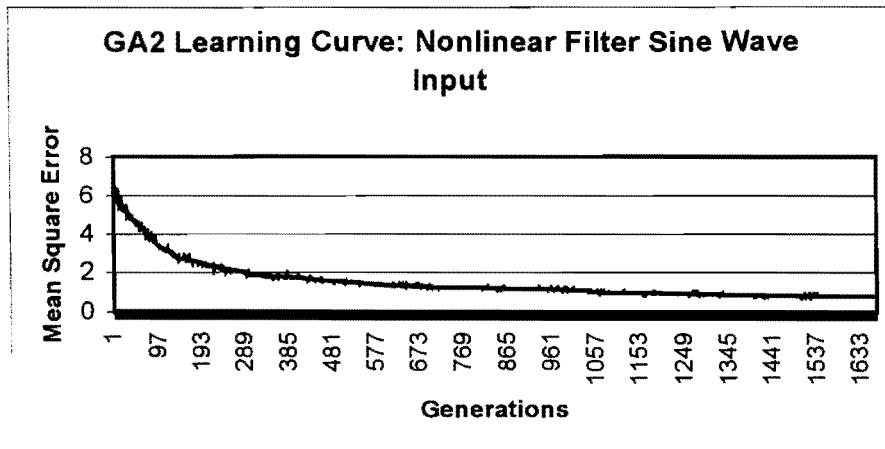


Figure 2: GA2 learning curve, nonlinear filter, sine wave input.

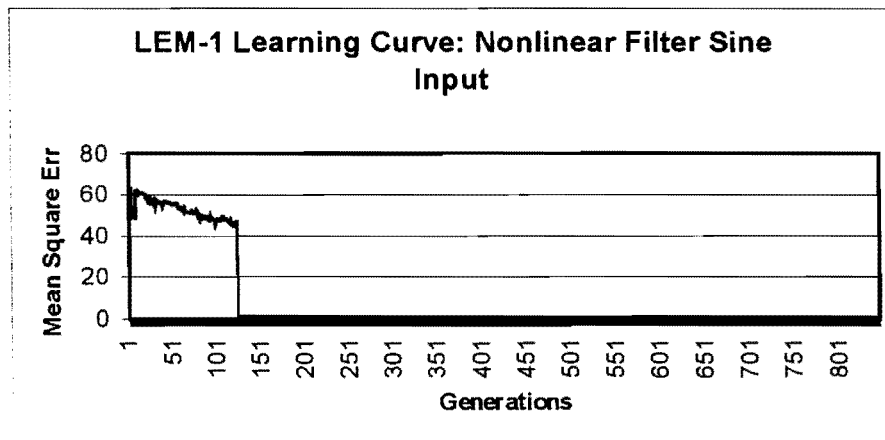


Figure 3: LEM-1 learning curve, nonlinear filter, sine input.

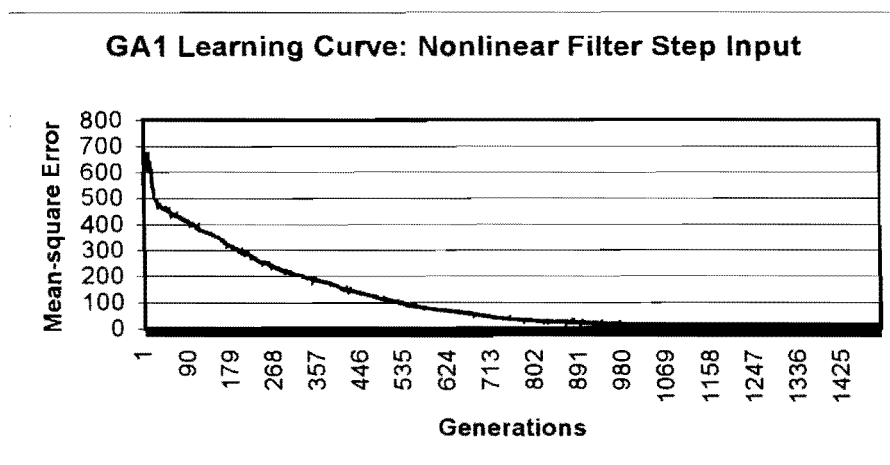


Figure 4: GA1 learning curve, nonlinear filter, unit step input.

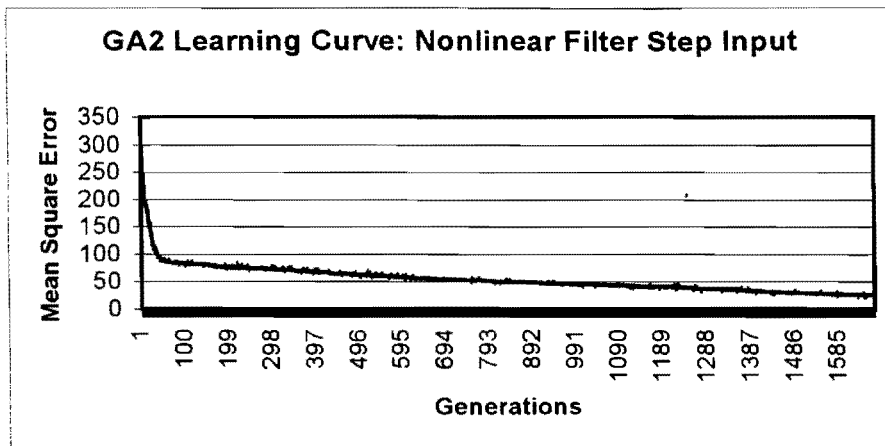


Figure 5: GA2 learning curve, nonlinear filter, unit step input.

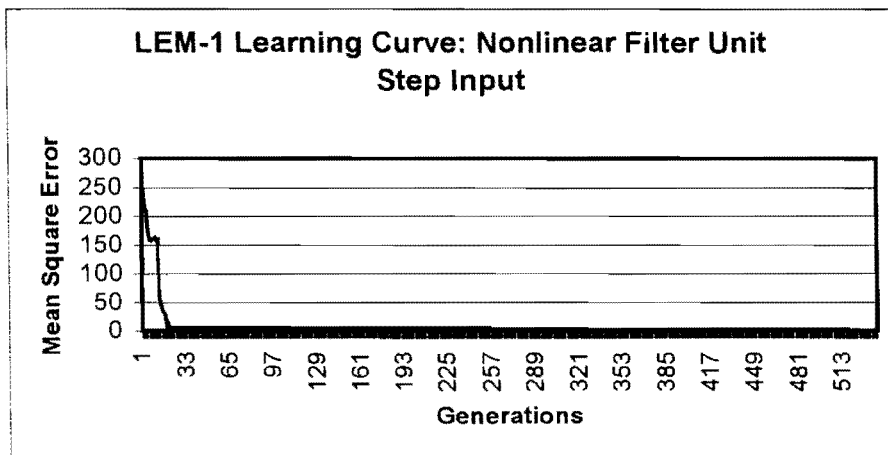


Figure 6: LEM-1 learning curve, nonlinear filter, unit step input

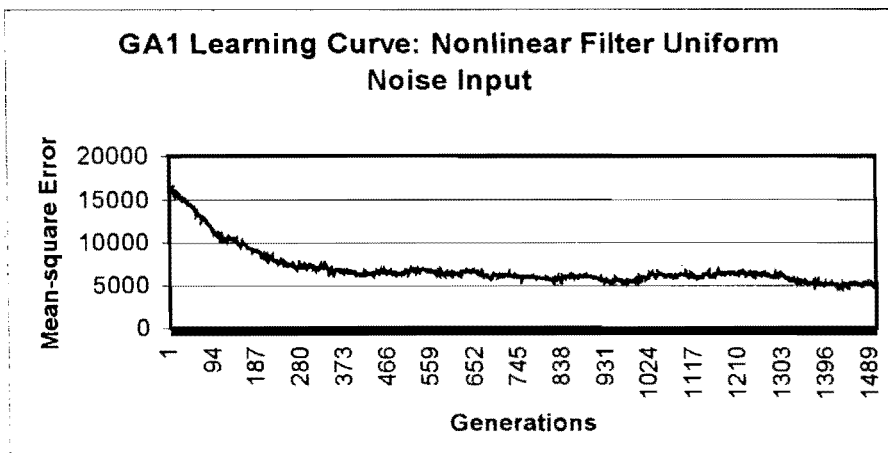


Figure 7: GA1 learning curve, nonlinear filter, uniform noise input.

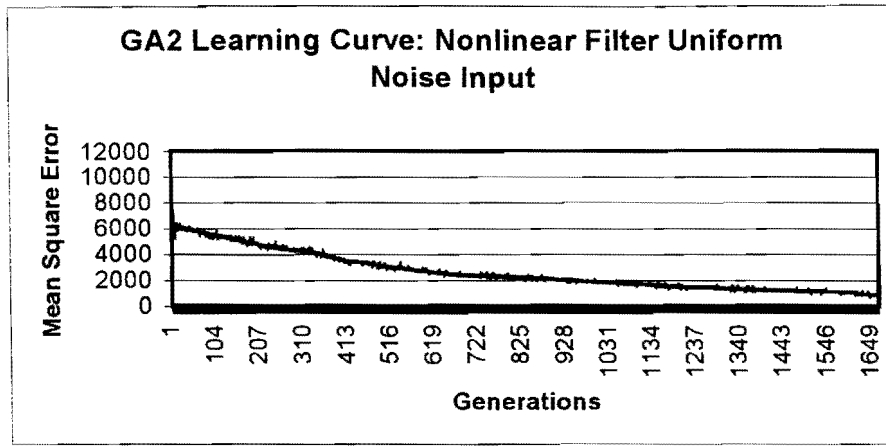


Figure 8: GA2 learning curve, nonlinear filter, uniform random noise input.

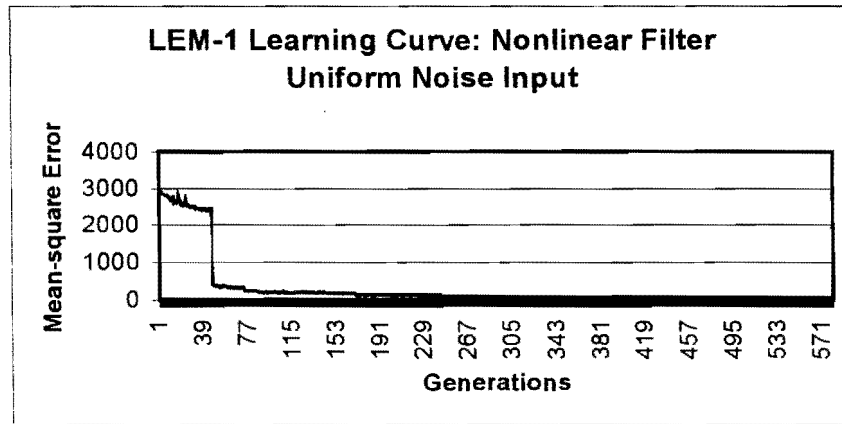


Figure 9: LEM-1 learning curve, nonlinear filter, uniform random noise input.

In the figures, the horizontal axis represents number of generations and the vertical axis represents the mean square error. As shown in the figures, in these experiments, LEM1 strongly outperformed GA1 and GA2 in terms of the speed of convergence. The effect of Machine Learning mode is demonstrated by a dramatic drop in the mean-square error when the system learned useful rules for generating the next generation of individuals. LEM1 toggled into Machine Learning mode roughly 10-800 times through out course of a typical experiment. A dramatic drop in mean-square error usually occurs within the first 100 generations.

Since we used four variables to represent the four weights of the filter, the error surface generated by the mean-square error is four-dimensional. Such an error surface creates difficulties for traditional search techniques. Such techniques, for example, the gradient descent and LMS, are prone to finding local minima. To achieve the robustness of the evolutionary

computation approach, they would have to explore solutions in parallel. LEM1 improves over evolutionary algorithms by accelerating the evolutionary process through a series of machine learning steps.

5 SUMMARY

This experimental study demonstrated that LEM1, a simple implementation of the LEM methodology, can produce significant speedups in the evolutionary process in comparison to conventional evolutionary algorithms. This speedup comes from Machine Learning mode that hypothesize rules characterizing differences between high and low performing individuals in consecutive populations. New populations are generated based on these rules. Thus, LEM generates new solutions using discovered patterns rather than stochastic operators employed in evolutionary algorithms. As described in (Michalski, 1999) these patterns can be viewed as qualitative differentials of the fitness landscape.

In our experiments, GA1, GA2, and LEM1 were applied to parameter estimation for non-linear filters for unit step, sine wave, and noisy input. In each case, LEM1 strongly outperformed GA1 and GA2 in terms of the number of generations needed to reach the optimal solution.

In conclusion, the LEM1 system has performed surprisingly well on the problem of parameter estimation for digital filters. It appears that the LEM approach is suitable for tackling complex search problems. Another practical problem areas where we expect the LEM approach to work well are function optimization problems and determining complex planning strategies.

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REFERENCES

- De Jong, K.A., An Analysis of the Behavior of a Class of Genetic Adaptive Systems, *Ph.D. Thesis*, Department of Computer and Communication Sciences, University of Michigan, Ann Arbor, 1975.
- Kaufman, K. and Michalski, R. S., The AQ18 System for Natural Induction: A User's Guide, *Reports of the Machine Learning and Inference Laboratory*, George Mason University, P98-11, October, 1998.
- Michalski, R. S., "AQVAL/1 -- Computer Implementation of a Variable-Value3d Logic System VL and Examples of its Application to Pattern Recognition," *Proceedings of the First International Joint Conference on Pattern Recognition*, Washington, D.C., pp. 3-17, October 30 - November 1, 1973.
- Michalski, R.S., "Learnable Evolution: Combining Symbolic and Evolutionary Learning," *Proceedings of the Fourth International Workshop on Multistrategy Learning (MSL '98)*, Desenzano del Garda, Italy, pp. 14-20, June 11-13, 1998.
- Michalski, R.S., "LEARNABLE EVOLUTION MODEL: Evolutionary Processes Guided by Machine Learning," *Reports of Machine Learning and Inference Laboratory*, MLI 99-3, 1999; to appear in *Machine Learning Journal*, 1999.
- Michalski, R.S., Mozetic, I., Hong, J. Lavrac, N., "The Multi-Purpose Incremental Learning System AQ15 and its Testing Application to Three Medical Domains," *Proceedings of the AAAI*, Philadelphia, August 11-15, 1986.
- Michalski, R.S. and Zhang, Q., Initial Experiments with Learnable Evolution Model: An Application of LEM1 to Function Optimization and Evolvable Hardware, *Reports of the Machine Learning and Inference Laboratory*, MLI 99-4, George Mason University, 1999.
- Wnek, J., Kaufman, K., Bloedorn, E. and Michalski, R.S., "Inductive Learning System AQ15c: The Method and User's Guide," *Reports of the Machine Learning and Inference Laboratory*, MLI 95-4, George Mason University, Fairfax, VA, March 1995.
- Yao, L. and Sethares, W., "Nonlinear Parameter Estimation via the Genetic Algorithm," *IEEE Transactions on Signal Processing*, Vol. 42 No.4 p.927-935. 1994.